

The impact of optimisation and machine learning on robotics

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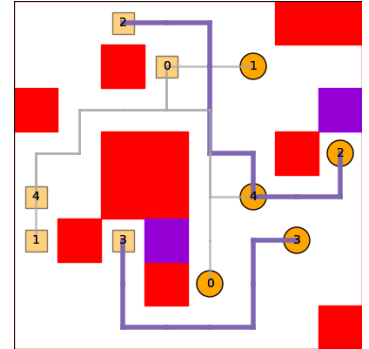
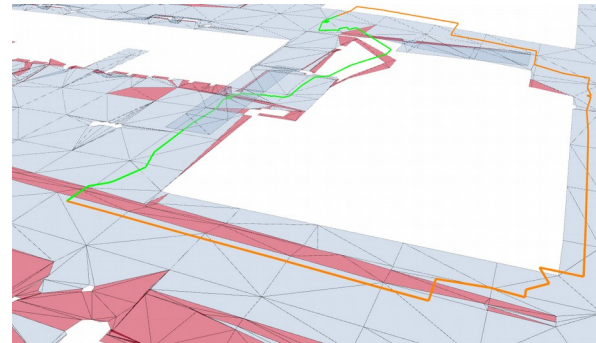
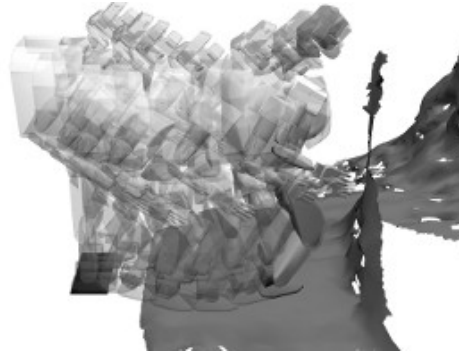
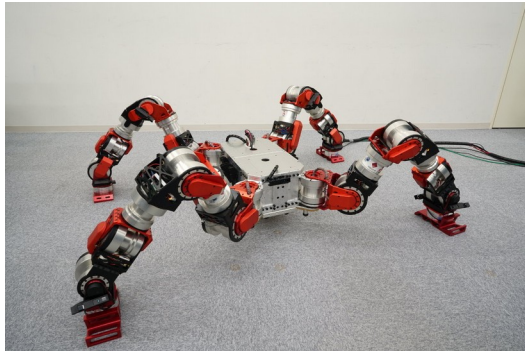
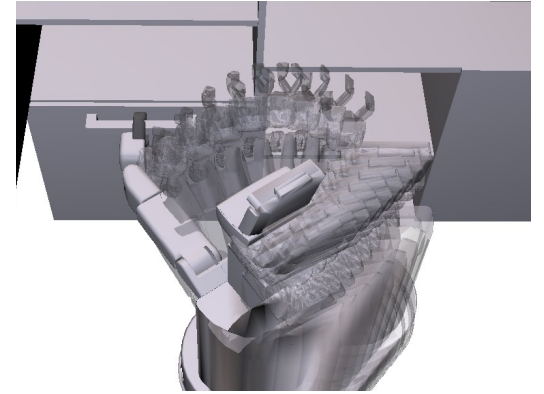
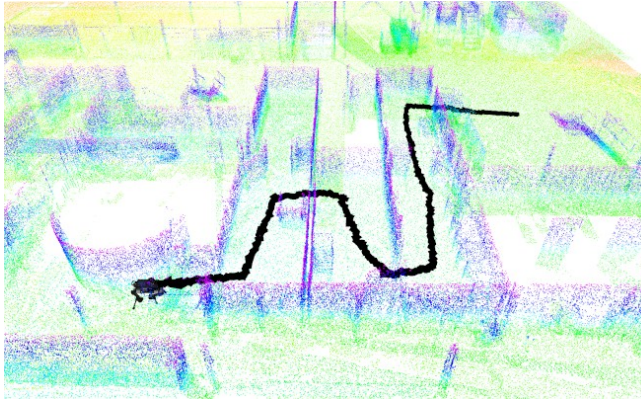
Responsible Robotics and AI lab

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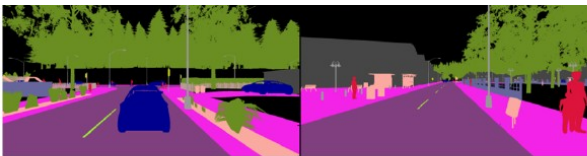
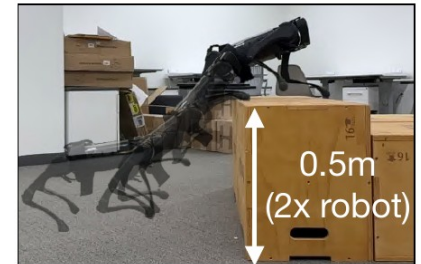
Safe and Trusted AI CDT

- Characterizing issues of Fairness, Accountability, Transparency, Ethics in AI
- New algorithms towards mitigating those issues

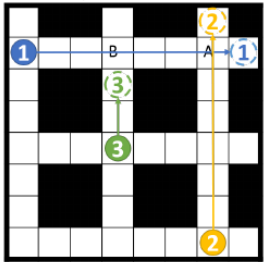
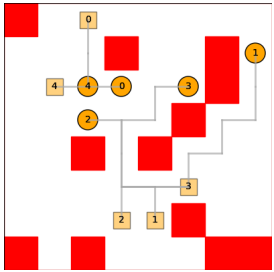
My background: Robotics



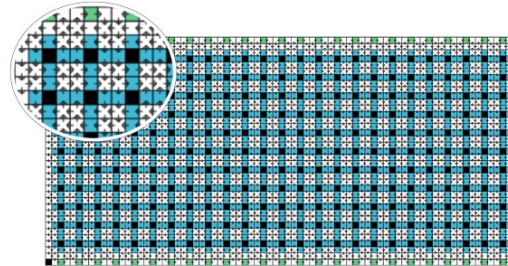
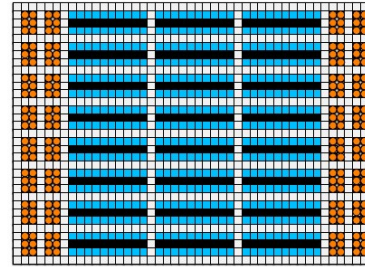
How has modern computing/AI/ML affected robotics?



Large-scale MAPF



Fast sub-optimal heuristics
(conflict resolution, prioritization,
symmetry-breaking...)



Dynamic robot locomotion

$$\underset{\Gamma}{\text{minimize}} \quad \sum_{k=1}^M L(\mathbf{q}[k], \mathbf{v}[k], \dot{\mathbf{r}}[k], \boldsymbol{\lambda}[k], h[k])$$

$$\text{subject to} \quad m\dot{\mathbf{r}}[k] = m\mathbf{g} + \sum_j \boldsymbol{\lambda}_j[k] \quad (\text{linear momentum})$$

$$\mathbf{k}[k] = \mathbf{A}_G^k(\mathbf{q}[k])\mathbf{v}[k] \quad (\text{angular momentum})$$

$$\dot{\mathbf{k}}[k] = \sum_j (\mathbf{c}_j[k] - \mathbf{r}[k]) \times \boldsymbol{\lambda}_j \quad (\text{angular momentum rate})$$

$$\forall_j \quad \boldsymbol{\lambda}_j[k] = \sum_{i=1}^{N_d} \beta_{ij}[k] \mathbf{w}_{ij} \quad (\text{friction})$$

$$\forall_{i,j} \quad \beta_{ij}[k] \geq 0$$

$$\mathbf{r}[k] = \text{COM}(\mathbf{q}[k]) \quad (\text{COM location})$$

Kinematic constraints

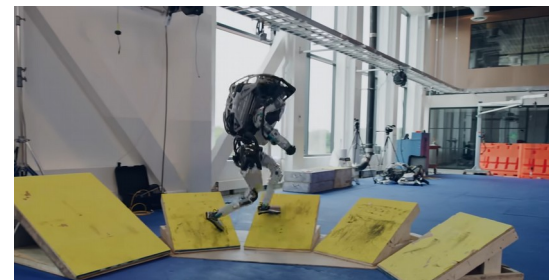
Time integration constraints



Full-body dynamics models,
on fast (commercial) optimization
solvers



Mastalli et al 2023 inverse-dynamics MPC via nullspace resolution

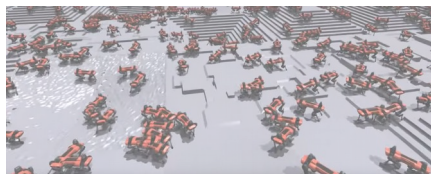
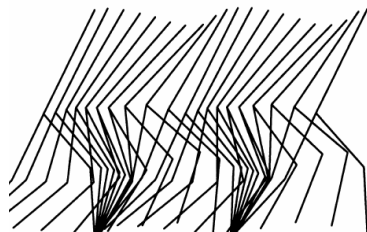


Boston Dynamics



Boston Dynamics

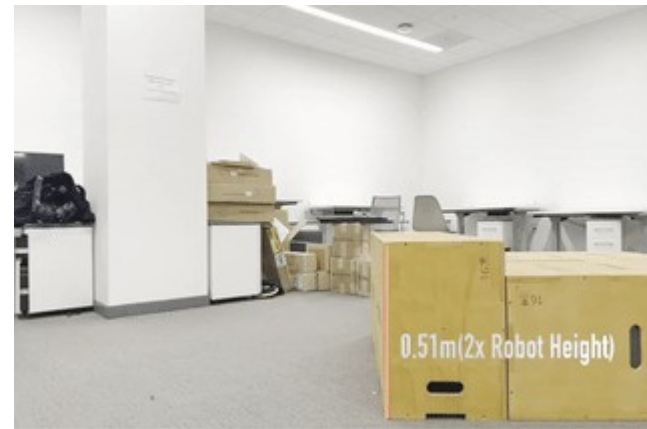
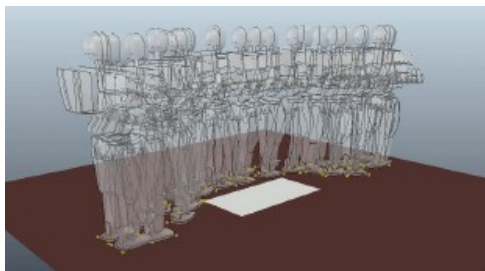
Robust & reactive motion



Rudin et al 2021 Learning to walk in minutes

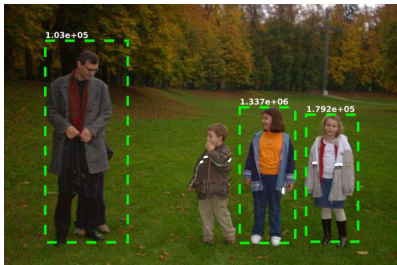


Reinforcement Learning
on large-scale GPU-accelerated
realistic simulation platforms



Cheng et al 2023 Extreme parkour with legged robots

Image understanding



Deep Neural Networks,
large-scale real datasets and
game-like realistic simulation
platforms



Wang et al 2022 SFNET-N



Schult et al 2023 Mask3D

BUT NOW WE HAVE...

Huge models

(DNNs, 3D robot/world models, full-body dynamics equations...)

Algorithms with lots of heuristics

(Convexification, symmetry-breaking, MIP, anytime suboptimal algos...)

Debugging and accountability problems

Need for explanation-generation algorithms ("XAI")

Explainability requirements for robot planning

Explain what?

Kinds of questions	Example questions
Plan-centered	why is this plan feasible? why is this plan infeasible? why is there no plan? (why did the planner fail to obtain a plan?) why did agents X traverse through locations L? why did agents X take paths Y, when I expected them to take path Z? why did agents X take paths that are so far off of paths Y? why did agents X wait/stop/get-precedence here? why did agents X wait for that other agent here? why did agents X wait for so long here? why is agent X not at location P before time T? why is agent X on a collision course? why is there a deadlock between agents X? why is there a congestion in area A?
Metric-centered	why isn't metric M higher? why is this plan optimal? why is this plan sub-optimal?
Consistency-centered	why does agent X always get precedence (over multiple problems)? why does agent X agent always go through location X (over multiple problems)? why is there always congestion in this area (over multiple problems)?
Algorithm-centered	why does heuristic H1 perform better than H2 in this problem/map? why does algorithm/variant A1 perform better than A2 in this problem/map? why does the algorithm take so long to find a path in this problem/map?
Design-centered	why do I need this many agents?

Explainability requirements

Kinds of explanations

Method-centered explanation

Because of the use of approximate collision checking
Because of the use of gradient methods on an unsmooth problem
Because the objective promotes solutions of following types
Because of the computation time budget used
Because hyper-parameter x is not y
Because of the algorithm's initialization scheme
Because the methods got stuck at an infeasible local minimum
Because cost weights are x not y
Because of chance
Because the algorithm did not obtain enough samples
Because of incorrect pruning of the search tree in state x
Because of the choice of planner
Because of a software bug

Problem-centered explanation

Because of conflicting constraints (x conflicts with y)
Because constraint x cannot be satisfied even by itself
Because of occupied space in region x (obstacle y)
Because of free space in region x
Because the robot dynamics has effect x
Because of the volume of robot part x
Because the problem has no solution
Because object x is not close enough
Because the start/waypoint/goal cannot be satisfied
Because the environment is cluttered
Because of a singularity in region x
Because path A is lower-cost
Because path A is safer/more-efficient
Because B is out of the workspace
Because path B crosses unmapped space
Because of a bug-trap in region x
Because of problem difficulty

Unknown

I dont know the reasons for x

Visualization-centered explanation

Visualize explored actions and their feasibility regions
Visualize where expected paths become infeasible
Visualize which part/link leads to not finding a plan and where
Visualize map/plan areas that are problematic/bottlenecks
Visualize with colours why the robot moved the way it did
Visualize families of good solutions coloured by performance

Most answers to “what kind of planner-generated explanations would be **useful**?” were problem- and visualization-centered.

Kinds of explanations

[multi-agent setting]

Table 3: Kinds of explanations for MAPF/MRMP
(I=Initial examples from interviewees; R=Refinements by questionnaire participants)

Category	Sub-category	Example explanations	I	R	
Plan-based	Agent interference	because that would delay agents X		*	
		because that would create conflicts with agents X		*	
		because of a deadlock between agents X	*	*	
	Event chains	because that would affect agent X, which would affect agent Y		*	
Landmarks		because of event X at time T that propagated	*	*	
		because a large number of agents have to go through area A	*	*	
	Problem-based	Problem properties	because the environment is not well-formed/well-structured	*	*
		Metric	because that would be worse according to the metric	*	*
		because that would require change X to the metric	*	*	
		because the metric would be the same	*	*	
	Constraints	because agents X have higher priority (imposed by the problem)	*	*	
		because that would require an extra constraint/precondition X	*	*	
		because of the kinodynamic constraints of agents X	*	*	
	Map	because of the costs assigned to edges/regions X	*	*	
		because object O is at location X	*	*	
		because of obstacles X	*	*	
		because of the size of the map	*	*	
		because of obstacle density (at location X)	*	*	
		because of a choke point at location X	*	*	
		because that would require a change to the map	*	*	
	Agents	because there are too many/few agents	*	*	
		because that would require X more/less agents	*	*	
		because that would require agents to have priorities X	*	*	
	Example	for the same reason as in this smaller problem	*	*	
Algorithm-based	Planner properties	because the planner does not provide safety guarantees	*	*	
		because the planner is incomplete	*	*	
		because the planner is sub-optimal	*	*	
		because heuristic H is inadmissible	*	*	
		because the planner is better on small/large maps	*	*	
		because the planner cannot handle a large number of agents well	*	*	
		because the planner explores movement in direction X first	*	*	
		because heuristic prefers moving agents close to their destination first	*	*	
		Planner decisions	because of an incorrect state expansion/prune	*	*
			because of planner-added constraint X (e.g. PBS, MAPF/C, k-delay MAPF)	*	*
	because of the priority ordering of the agents (imposed by planner)		*	*	
	Planner parameters	because algorithm A1 was used instead of A2	*	*	
		because heuristic H1 was used instead of H2	*	*	
	Information	because hyperparameter X was equal/lower/higher than Y	*	*	
		because of incorrect information (decentralized algorithms)	*	*	
		because of insufficient information (decentralized algorithms)	*	*	
	Bug	because the algorithm was not trained on similar examples (learning algorithms)	*	*	
because of a bug in function/class/file/line X		*	*		
Execution-based	Execution gap	because agents X stopped due to technical failure	*	*	
		because agents X are moving slower/faster than expected	*	*	

Explainability use-cases

In motion planning

- **Warehouse automation**

- Large-scale (1000s agents), dynamic, anytime sub-optimal planners.
- Explanations could **help developers** tune cost functions, **onsite engineers** add constraints/params on the fly, **layout designers** improve layout

- **Computer games**

- Large-scale, dynamic, sub-optimal planners, no safety guarantees.
- Explanations could **help game designers** understand reasons for undesired behavior, know what to change to improve game.

- **Mining**

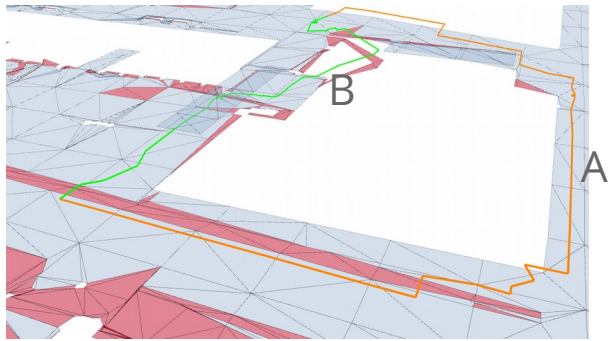
- Continuous, kinodynamic, uncertainty-aware, distributed planners.
- Explanations could **help managers** understand why metrics are being optimized.

- **All applications**

- Explanations could **help developers and researchers** inspect models and algorithms, find bugs, understand why some heuristic/parameters/variants work better than others.

Explainable path planning

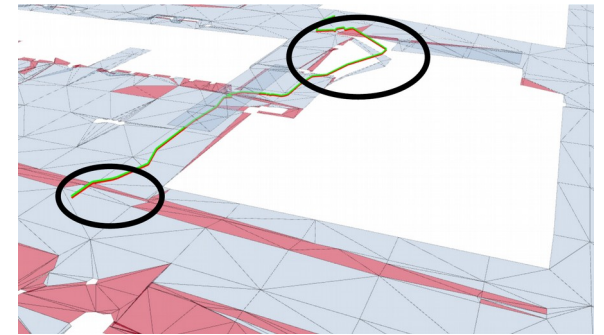
Problem-centred explanations



Why plan A, instead of B which I expected?

$$\begin{array}{ll}
 \min_{l', \pi, \lambda} & \|l' - l\|_1 \\
 \text{s.t.} & \sum_i A_{ij} \pi_i = \sum_k d_j c_k l'_{k,r(j)} \quad \forall j: x'_j = 1 \\
 & \sum_i A_{ij} \pi_i + \lambda_j = \sum_k d_j c_k l'_{k,r(j)} \quad \forall j: x'_j = 0 \\
 & \pi \in \mathbb{R}^{|V|} \\
 & \lambda \in \mathbb{R}^{|E|} \\
 & \lambda_j \geq 0 \quad \forall j: x'_j = 0 \\
 & l' \in \{0, 1\}^{K|V^r|} \\
 & \sum_k l'_{k,i} = 1 \quad \forall i,
 \end{array}$$

Terrain-MILP:



“Because these areas are high-cost”

$$\begin{array}{ll}
 \min_{c', \pi, \lambda} & \|c' - c\|_1 \\
 \text{s.t.} & \sum_i A_{ij} \pi_i = \sum_k d_j c'_k l_{k,r(j)} \quad \forall j: x'_j = 1 \\
 & \sum_i A_{ij} \pi_i + \lambda_j = \sum_k d_j c'_k l_{k,r(j)} \quad \forall j: x'_j = 0 \\
 & \pi \in \mathbb{R}^{|V|} \\
 & \lambda \in \mathbb{R}^{|E|} \\
 & \lambda_j \geq 0 \quad \forall j: x'_j = 0 \\
 & c' \in \mathbb{R}_+^K,
 \end{array}$$

COT-MILP:

“Because blue areas are too low cost compared to red”

Explainable road navigation

Problem-centred explanations



Shortest Path
 $x = \operatorname{argmin} w.x$

$$\begin{aligned} & \text{minimize} && \|n' - n\|_1 + \|c' - c\|_1 + \|b^s\|_1 + \|b^{m'}\|_1 \\ & n', c', b^s, b^{m'}, \pi, \lambda && \end{aligned} \quad (5a)$$

$$\begin{aligned} & \text{subject to} \\ & \sum_i A_{ij} \pi_i = s'_j l_j + n'_j M + c'_j M, \quad \forall_{j: x'_j = 1 \wedge m_j / s_j < r',} && (5b) \\ & \sum_i A_{ij} \pi_i = m'_j l_j + n'_j M + c'_j M, \quad \forall_{j: x'_j = 1 \wedge m_j / s_j \geq r',} && (5c) \\ & \sum_i A_{ij} \pi_i + \lambda_j = s'_j l_j + n'_j M + c'_j M, \quad \forall_{j: x'_j = 0,} && (5d) \\ & \lambda_j \geq 0, \quad \forall_{j: x'_j = 0,} && (5e) \\ & n'_j = n_j, \quad c'_j = c_j, \quad \forall_{j: x'_j = 1 \wedge x'_j = 0,} && (5f) \\ & n'_j = 0, \quad c'_j = 0, \quad \forall_{j: x'_j = 1,} && (5g) \\ & n' \in \{0, 1\}^{|E|}, \quad c' \in \{0, 1\}^{|E|}, \quad b^s \in \{0, 1\}^{|E|}, \\ & b^{m'} \in \{0, 1\}^{|E|}, \quad \lambda \in \mathbb{R}^{|E|}, \quad \pi \in \mathbb{R}^{|V|}, && (5h) \end{aligned}$$

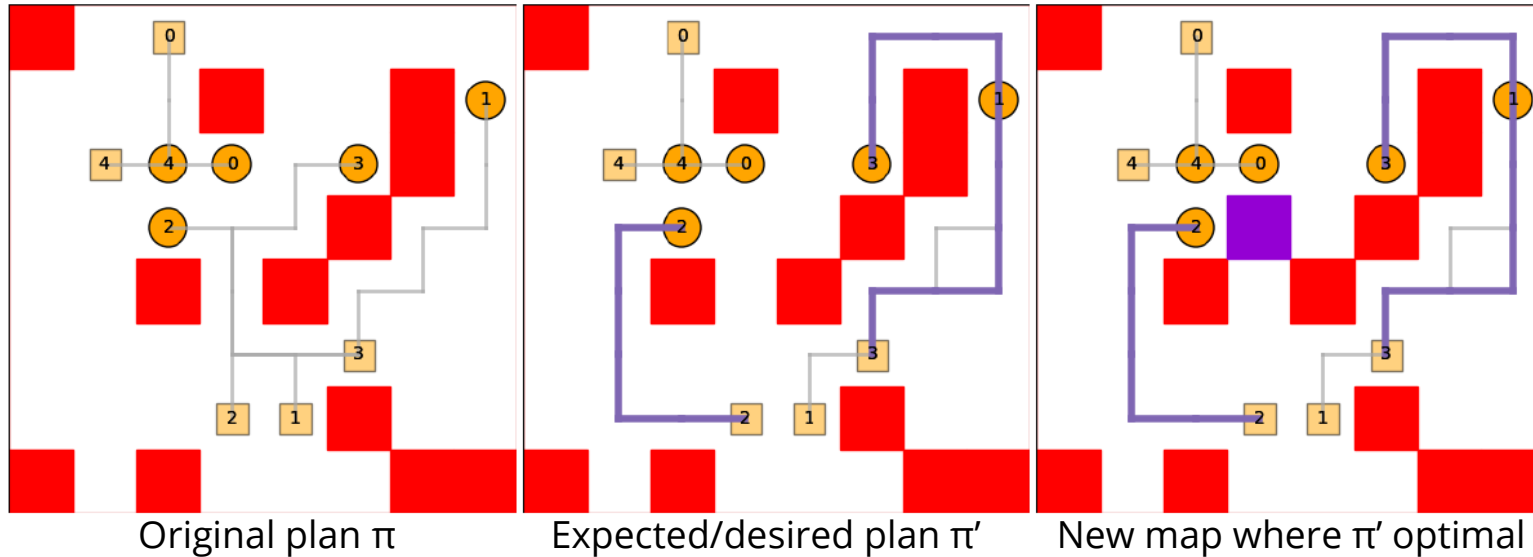
$n', c', b^s, b^{m'}$

“The desired path is not optimal because **Endell Street** is currently closed; and **Long Acre** is a one-way road.”

$c'_{\text{EndellStreet}} = 0$; $n'_{\text{LongAcre}} = 0$
 (i.e. these changes make x' optimal)

Explainable multi-agent planning

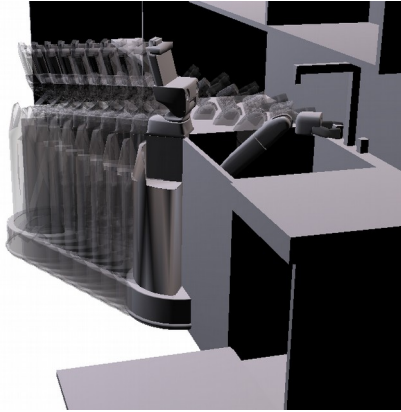
Problem-centred explanations



“why not π' instead of π ?”

→ “because the cells in
purple are free
(but if they were occupied then
 π' would be optimal)”

Explainable motion planning



Why did you fail?



Problem-centred explanation

Algorithm 1 (constraint-based failure explanation):
1: for each \mathcal{H}_i in $\mathcal{P}(\mathcal{H})$:
2: $\xi_i = \operatorname{argmin}_{\xi} C[\xi] + \mathbf{1}_{H_{\text{target}} \in \mathcal{H}_i} \alpha C_{\text{target}}[\xi]$ s.t. \mathcal{H}_i
3: $k = \operatorname{argmin}_i C[\xi_i] - \beta |\mathcal{H}_i| + \gamma C_{\text{target}}[\xi_i]$ s.t. $H_{\text{collision}}$
4: return Message("Not all constraints could be satisfied. The problem would be feasible if constraints $\mathcal{H} \setminus \mathcal{H}_k$ were dropped and the target was $C_{\text{target}}[\xi_k]$ meters away from the original.")

Because constraints "target" and "collision" conflict with each other. The problem would be feasible if the target was 0.15m away.



Algorithm-centred explanation

Algorithm 2 (initialization-based failure explanation):
1: for $i = 1, \dots, N_{\text{max}}$:
2: Pick random initialization and use it below
3: $\xi_i = \operatorname{argmin}_{\xi} C[\xi]$ s.t. \mathcal{H}
4: if ξ_i :
5: return Message("The initialization was in the basin of attraction of an infeasible local minimum. The planner would succeed with initialization ξ_i .")
6: else:
7: return Message("Unfeasible or hard problem for random initialization.")

Because the initialization was in the basin of attraction of an infeasible local minimum. The planner would have succeeded with a random initialization policy.



NOW WE HAVE...

Huge models

(DNNs, 3D robot/world models, full-body dynamics equations...)

Algorithms with lots of heuristics

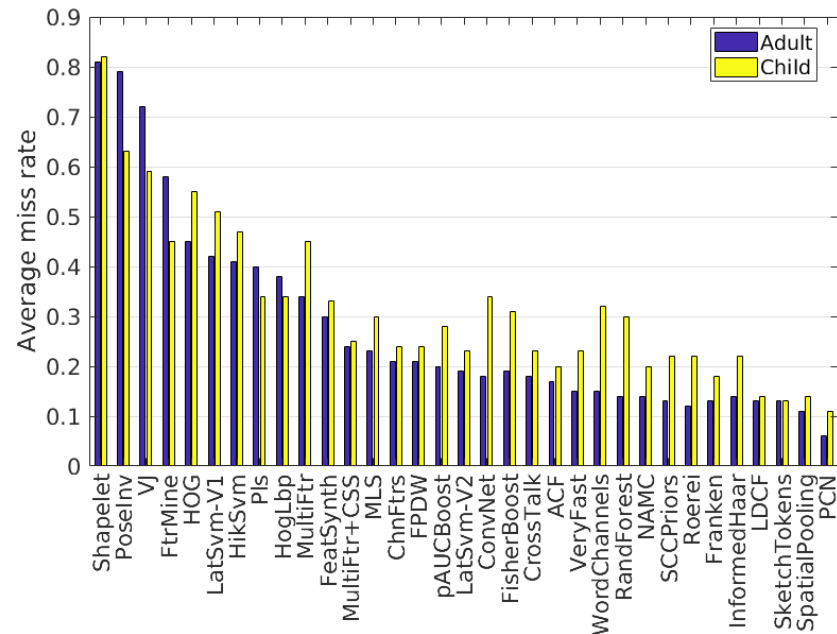
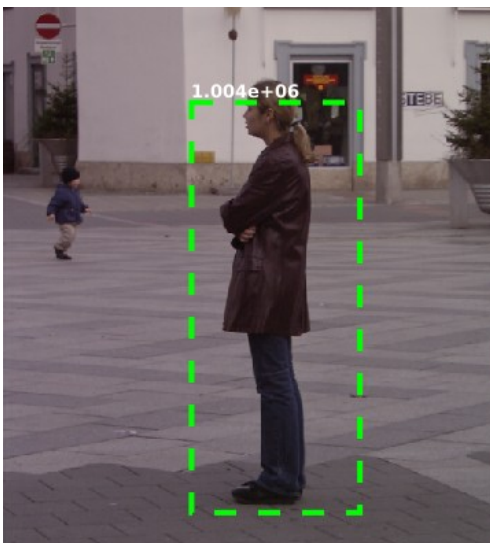
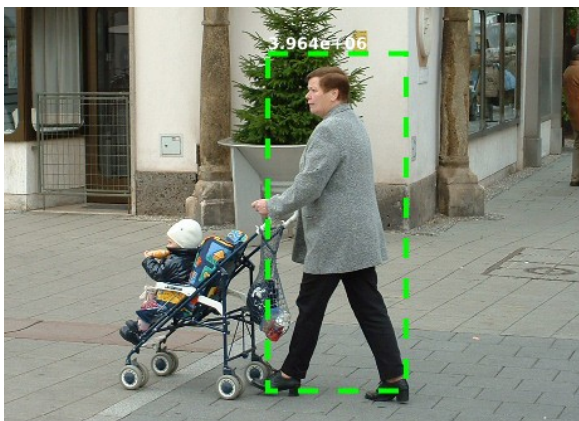
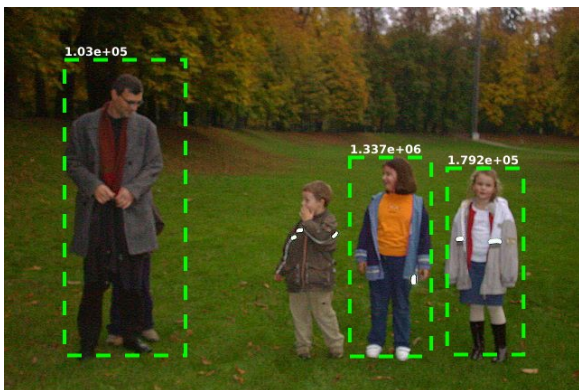
(Convexification, symmetry-breaking, MIP, anytime suboptimal algos...)

Debugging and accountability problems

Also: algorithmic bias problems

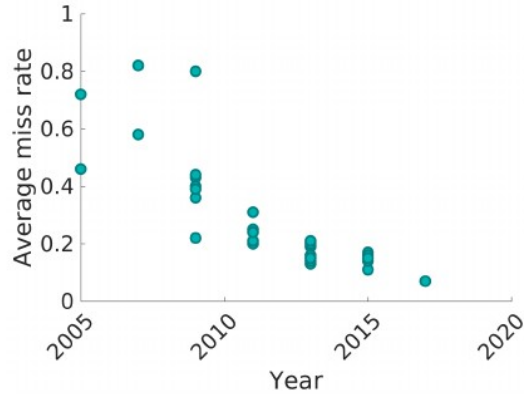
In robotics: biased models → biased physical safety

Bias in pedestrian detection?

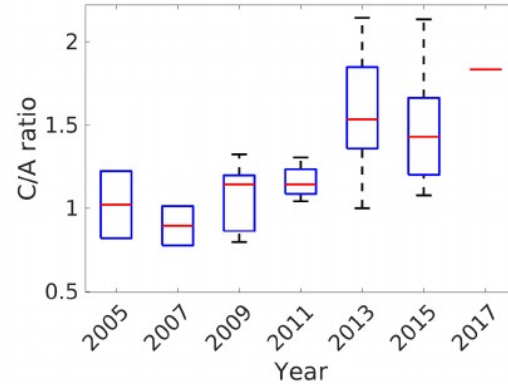


- **All top-24** methods have **higher miss rates on children**.
- Best methods almost **2x miss rates** on children vs adults.
- **Physical safety** differences

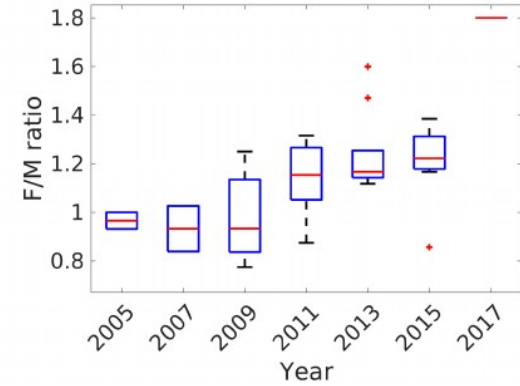
Pedestrian detection trends



Miss rates going down



Disparity going up



Disparity going up

Increase in **average performance** + Increase in **performance gap** (majority-minority)

Need bias mitigation methods, overfitting avoidance

Conclusion

- **Robots have become:** more dynamic, robust, adaptive, large-scale interaction-ready, world-understanding
- **Thanks to:** large physics models, fast optimization solvers, heuristics, large simulated worlds, large neural networks
- **With disadvantages:** difficulties in debugging, predictability, explainability; growing issues of bias on minorities

Still some work to do...

Thank you