

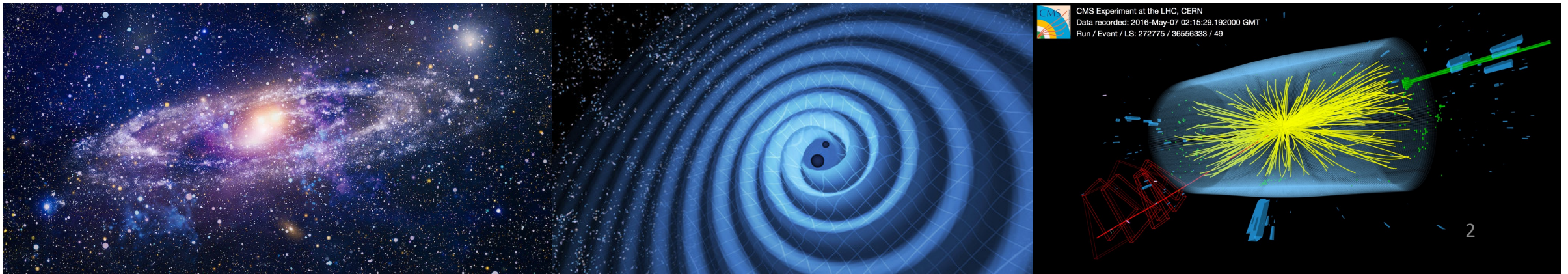
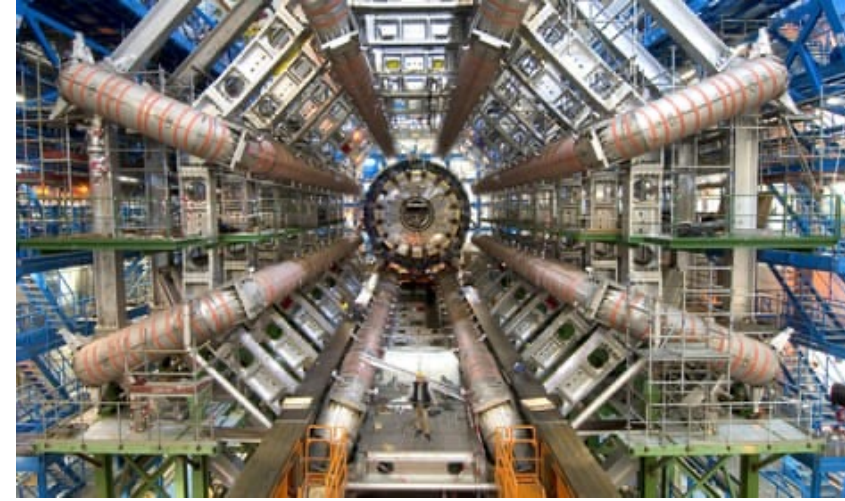
ML in fundamental physics

Gert Aarts



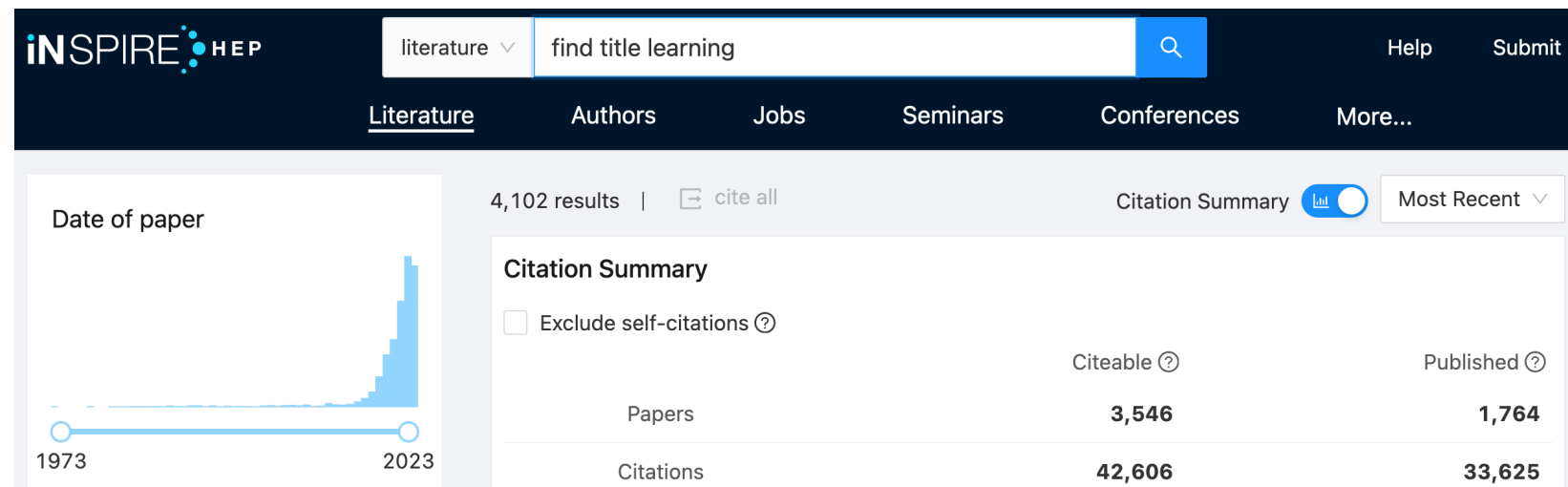
Fundamental physics

- understood to mean **particle physics** and **astronomy**
- big questions about the very small: **elementary particles, quarks and gluons** and the very large: **galaxies, black holes, gravitational waves, the universe**
- no immediate application in society, but long-term interest (and impact!) in understanding nature



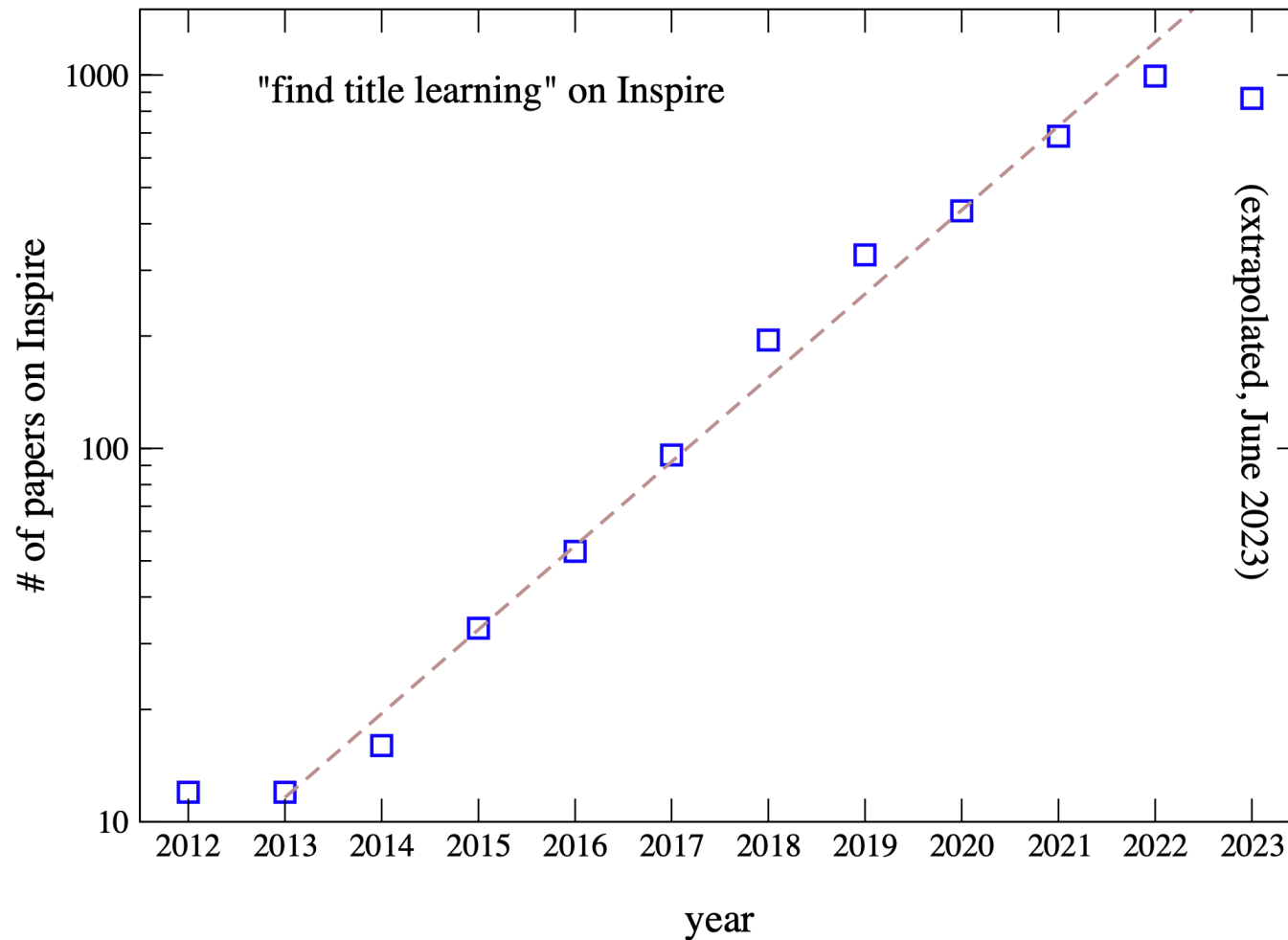
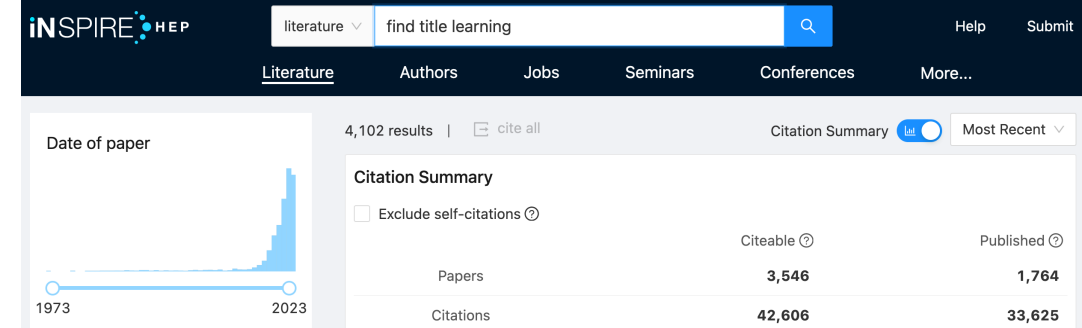
High-energy physics (HEP)

- past seven years or so have seen a rapid rise of applications of ML
- of course, ML has been around for quite some time, especially in experimental particle physics
- nevertheless, there is an **exponential** increase in activity



“find title **learning**” on the iNSPIRE-HEP data base
dedicated HEP database, collecting all papers in the field

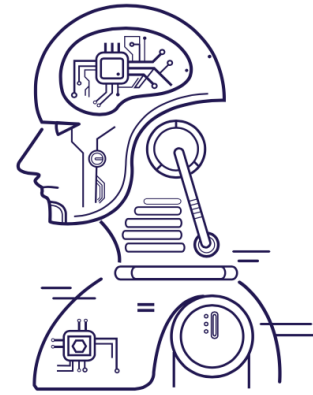
High-energy physics (HEP)



find title **learning**
on the iNSPIRE-HEP
data base

exponential increase

AIMLAC



UKRI CENTRE FOR DOCTORAL TRAINING
IN ARTIFICIAL INTELLIGENCE, MACHINE
LEARNING AND ADVANCED COMPUTING

- 60% particle physics/astronomy
- 25% computer science/maths
- 15% health



AIMLAC: some project titles

- coevolution of galaxies and supermassive black holes in the Euclid era
- searching for New Physics with the CMS experiment at the Large Hadron Collider
- a cold and dusty universe: understanding the cosmic dust and cold gas in nearby galaxies
- tests of the dark sector with gravitational waves
- exploiting GAIA data and understanding the galaxies' past histories with ML
- simulation-based inference of gravitational waves signals from black holes and neutron stars
- searches for Beyond-Standard-Model signatures with jets + missing energy
- monsters in the dark: gas, dust and star formation around supermassive black holes
- AI techniques for extracting source information from Square Kilometre Array (SKA) datasets
- deep learning for real-time gravitational wave detection
- ...

ML in fundamental physics

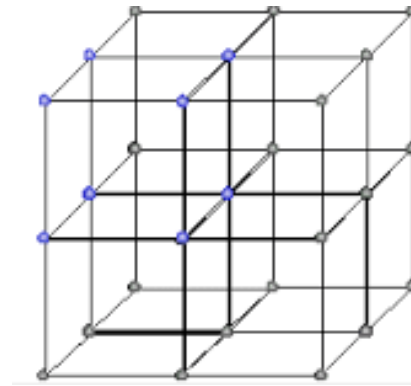
- lots of applications of ML in particle physics, astronomy, gravitational waves, ...

AI/ML for physics

- considerable overlap between concepts in theoretical physics and in ML
- interesting cross-talk to explore algorithms and improve understanding

physics for AI/ML

My interests and background

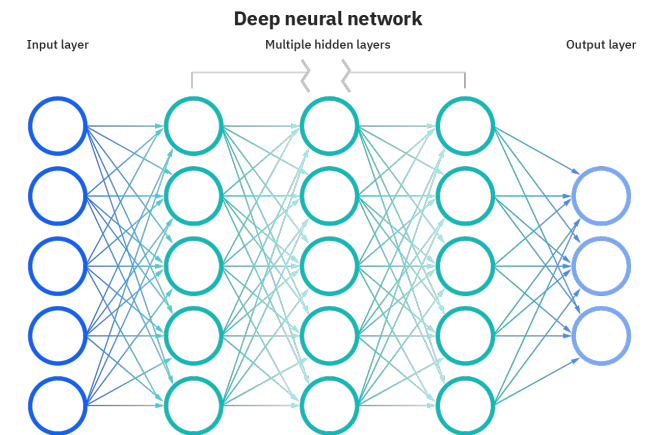


theoretical physics → particle physics → quantum field theory → lattice field theory

- understand the strong nuclear force (quarks & gluons) from first principles
- systems of many fluctuating degrees of freedom (quantum fields) on a spacetime lattice
- interactions via fluctuating links, determined by physical theory

ML models/neural networks

- train ML model to complete some task
- many degrees of freedom (“neurons”) on a multi-layered network
- nodes interact via weights, determined by loss function



Conceptual and practical questions

can experience in quantum field theory help in understanding ML and vice versa?

- quantum field-theoretic machine learning

Dimitrios Bachtis, GA, Biagio Lucini, Phys. Rev. D 103 (2021) 074510 [[2102.09449](#)] [hep-lat]

- scalar field restricted Boltzmann machines as an ultraviolet regulator

Chanju Park, Biagio Lucini, GA, [2309.15002](#) [hep-lat]

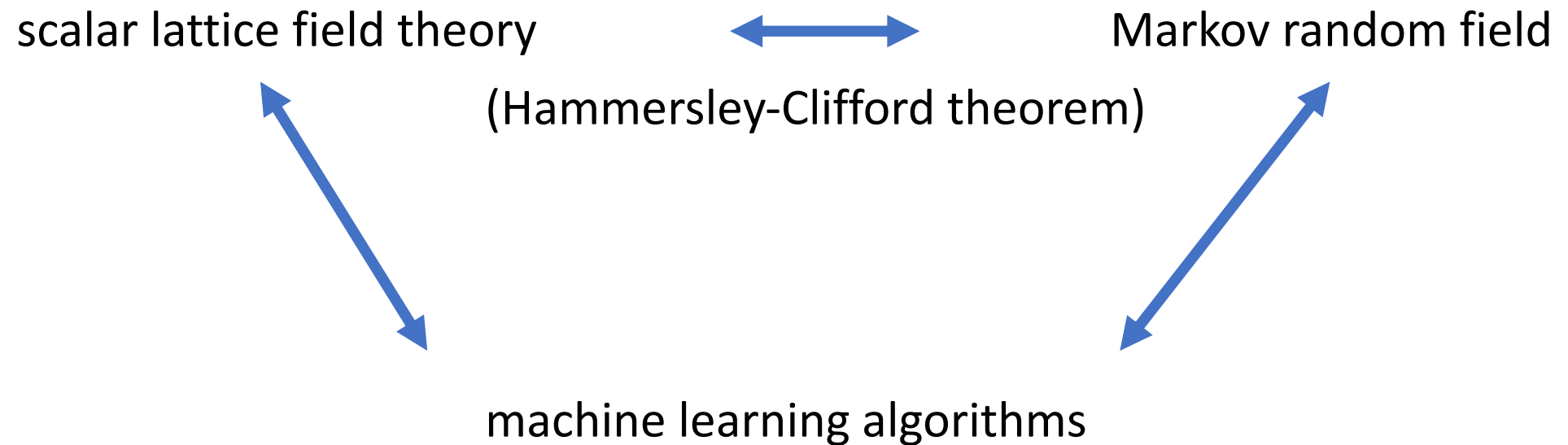
- stochastic quantisation and diffusion models

Lingxiao Wang, GA, Kai Zhou, [2309.17082](#) [hep-lat]

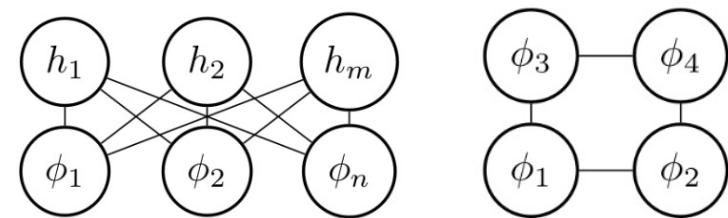
NeurIPS 2023 [2311.03578](#) [hep-lat]

lattice field theory and Markov random fields

derive machine learning algorithms from discretized Euclidean field theories



Probability distribution $p(\varphi)$



probability distribution $p(\varphi)$ defined as product of nonnegative functions over maximal cliques in graph (or lattice):

$$p(\phi) = \frac{1}{Z} \prod_{c \in C} \psi_c(\phi)$$

then $p(\varphi)$ satisfies local Markov property

and set of random variables φ define a Markov random field

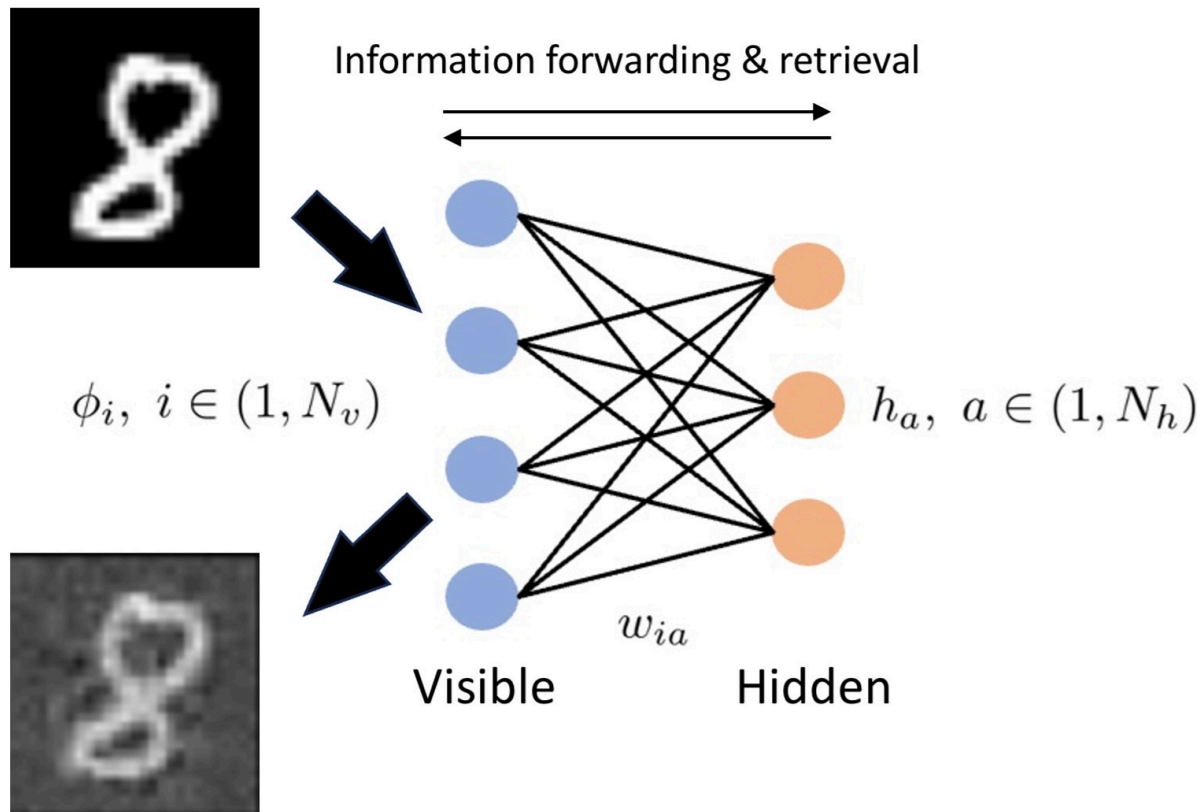
$p(\varphi)$ defines lattice field theory

Theorem 1 (Hammersley-Clifford.) *A strictly positive distribution p satisfies the local Markov property of an undirected graph \mathcal{G} , if and only if p can be represented as a product of nonnegative potential functions ψ_c over \mathcal{G} , one per maximal clique $c \in C$, i.e.,*

$$p(\phi) = \frac{1}{Z} \prod_{c \in C} \psi_c(\phi), \quad (2)$$

where $Z = \int_{\phi} \prod_{c \in C} \psi_c(\phi) d\phi$ is the partition function and ϕ are all possible states of the system.

Restricted Boltzmann Machine: generative network

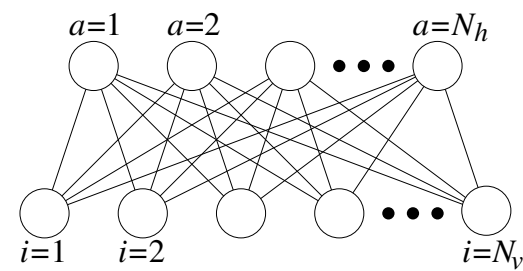


- energy-based method
- probability distribution
- binary or continuous d.o.f.

$$p(\phi, h) = \frac{1}{Z} e^{-S(\phi, h)}$$

$$Z = \int D\phi D h e^{-S(\phi, h)}$$

Scalar field RBM



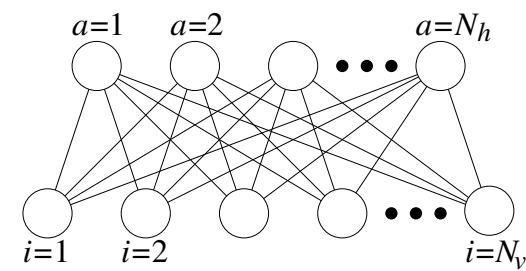
- treat RBM as a **lattice field theory** with action

$$S(\phi, h) = \sum_i \frac{1}{2} \mu_i^2 \phi_i^2 + \sum_a \frac{1}{2\sigma^2} (h_a - \eta_a)^2 - \sum_{i,a} \phi_i w_{ia} h_a$$

- only quadratic terms: learn weight matrix w_{ia} and bias η_a
- induced distribution on visible layer

$$p(\phi) = \int Dh p(\phi, h) = \frac{1}{Z} \exp \left(-\frac{1}{2} \sum_{i,j} \phi_i K_{ij} \phi_j + \sum_i J_i \phi_i \right)$$

- kinetic (all-to-all) term $K_{ij} = \mu_i^2 \delta_{ij} - \sigma^2 \sum_a w_{ia} w_{aj}^T$ and source $J_i = \sum_a w_{ia} \eta_a$

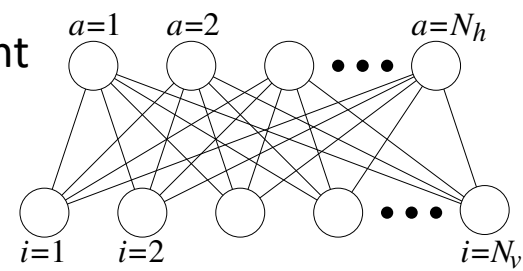


Gaussian scalar field RBM

- kinetic (all-to-all) term $K_{ij} = \mu_i^2 \delta_{ij} - \sigma^2 \sum_a w_{ia} w_{aj}^T$ and source $J_i = \sum_a w_{ia} \eta_a$
- kinetic term and source should match target distribution/data
- for instance: target is scalar field theory with $K\phi \approx p^2 + m^2$
- ❖ dependence on N_h : what if $N_h < N_v$? role of hyperparameter μ^2 ?
- ❖ both N_h and μ^2 act as **ultraviolet regulators**
- regulate the spectrum of the quadratic operator $K\phi$ of the target distribution/data

What if $N_h < N_v$?

train RBM with persistent
contrastive divergence

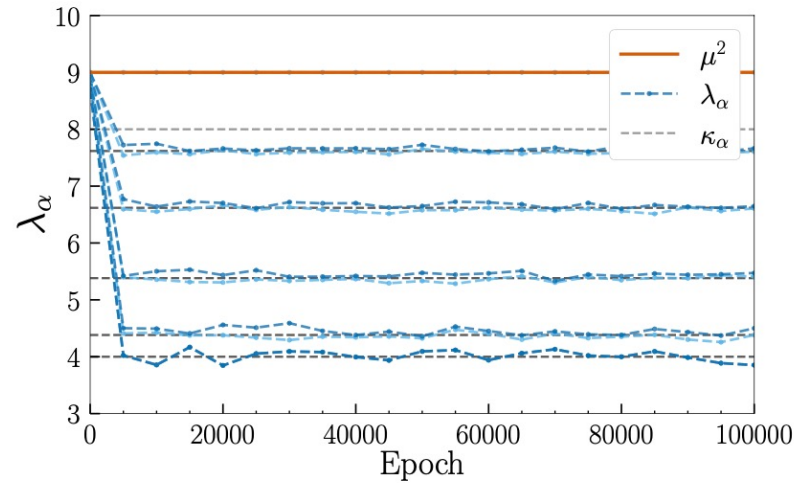


- example: scalar LFT
with $N_v = 10$ nodes

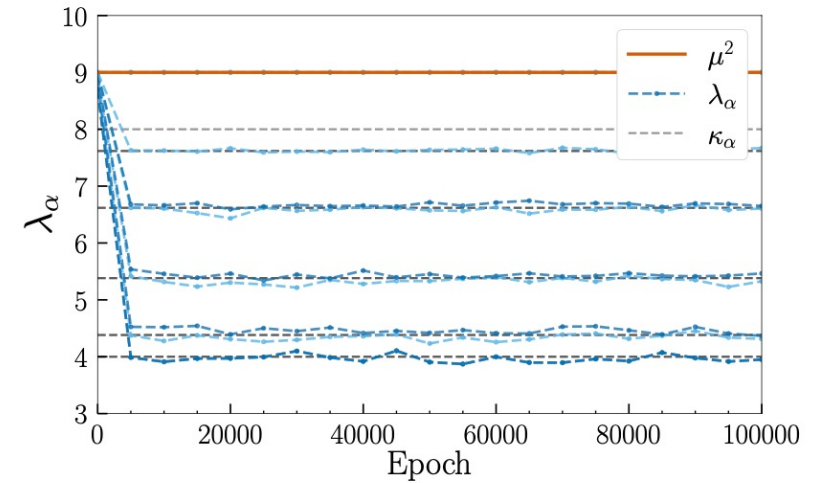
- exact spectrum:

$$\kappa \sim p^2 + m^2$$

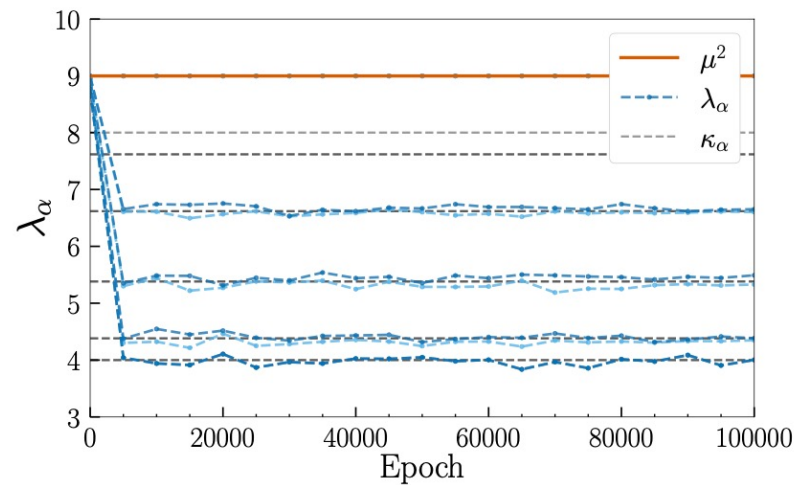
- reproduced by RBM (λ) from
smallest eigenvalue upwards
- higher modes are moved to
cut-off scale (μ^2)



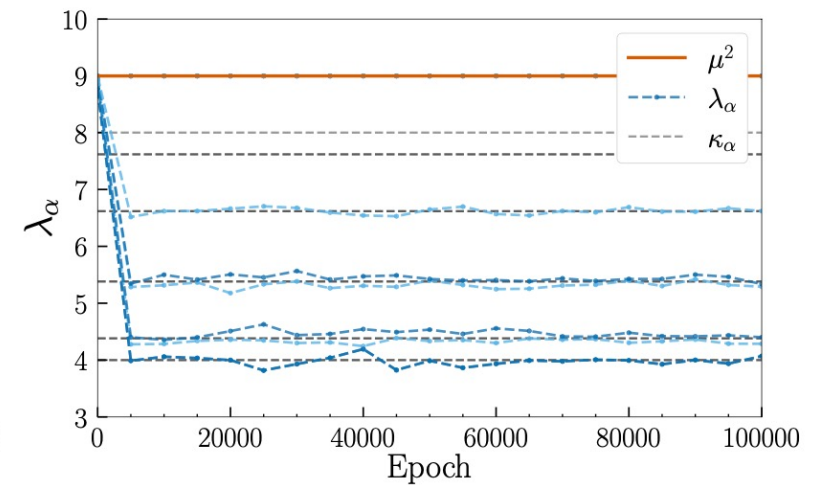
(a) $N_h = 9$



(b) $N_h = 8$

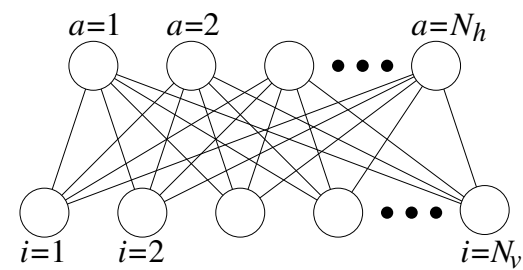


(c) $N_h = 7$



(d) $N_h = 6$

What if RBM parameter $\mu^2 < \lambda_{max}$?



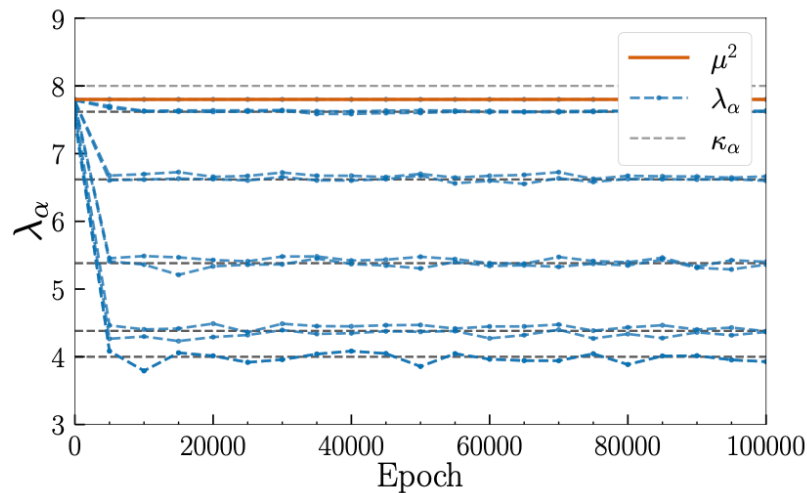
- example: scalar LFT with $N_v = 10$ nodes

- exact spectrum:

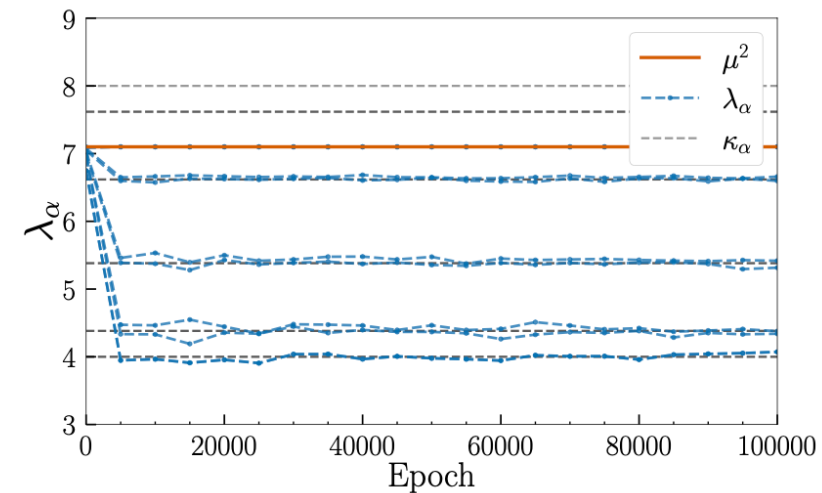
$$\kappa \sim p^2 + m^2$$

- reproduced by RBM (λ) from smallest eigenvalue upwards

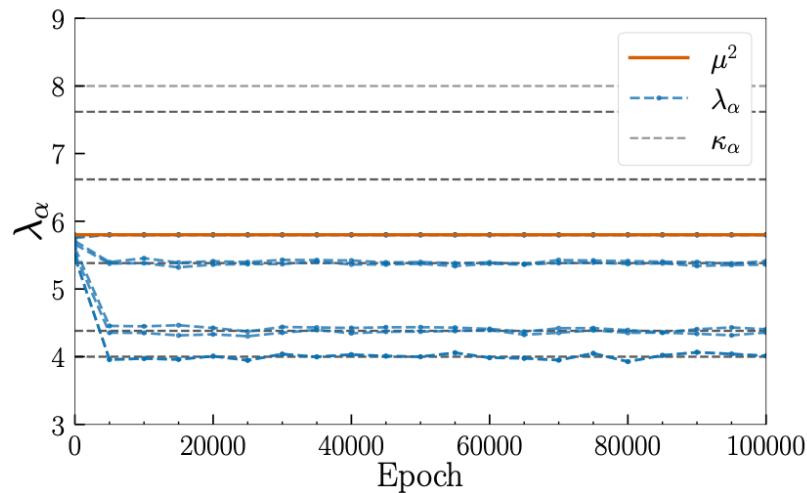
- higher modes are suppressed at cut-off scale (μ^2)



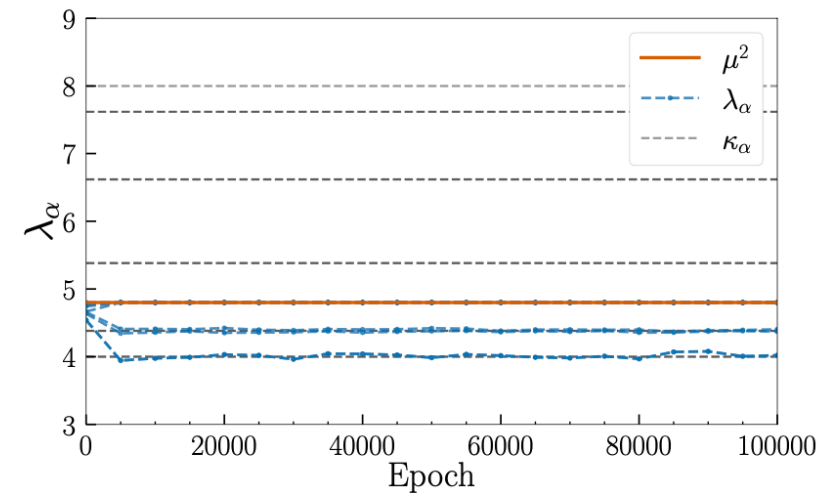
(a) $\mu^2 = 7.8$



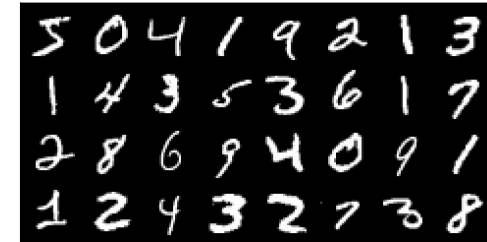
(b) $\mu^2 = 7.1$



(c) $\mu^2 = 5.8$

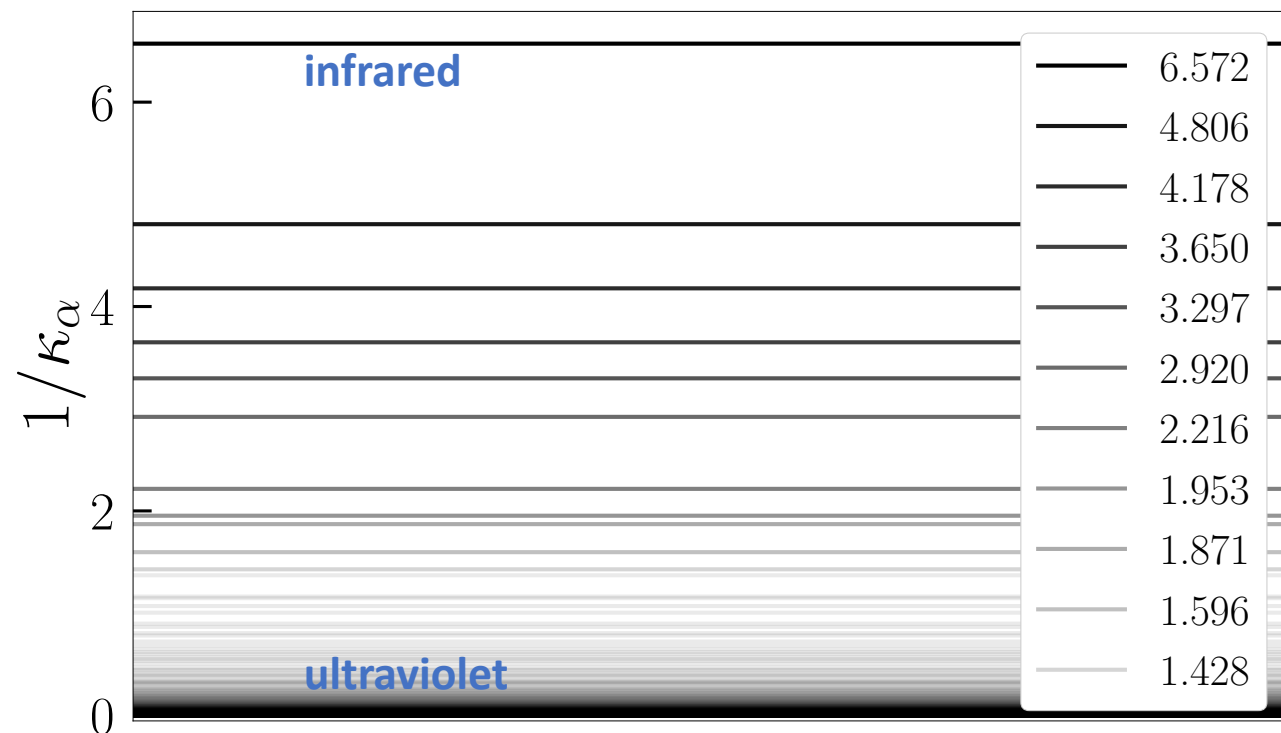


(d) $\mu^2 = 4.8$

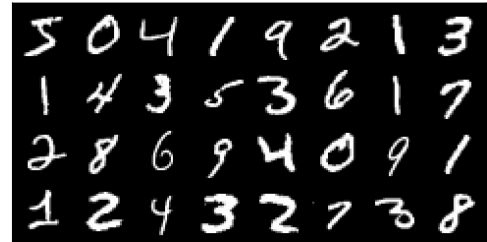


RBM as ultraviolet regulator

- relevant for “real” data sets? MNIST
- compute spectrum of two-point correlator $K_{ij}^{-1} = \langle \phi_i \phi_j \rangle_{data}$
- inverse spectrum $1/\kappa$
- infrared safe
- ultraviolet divergent

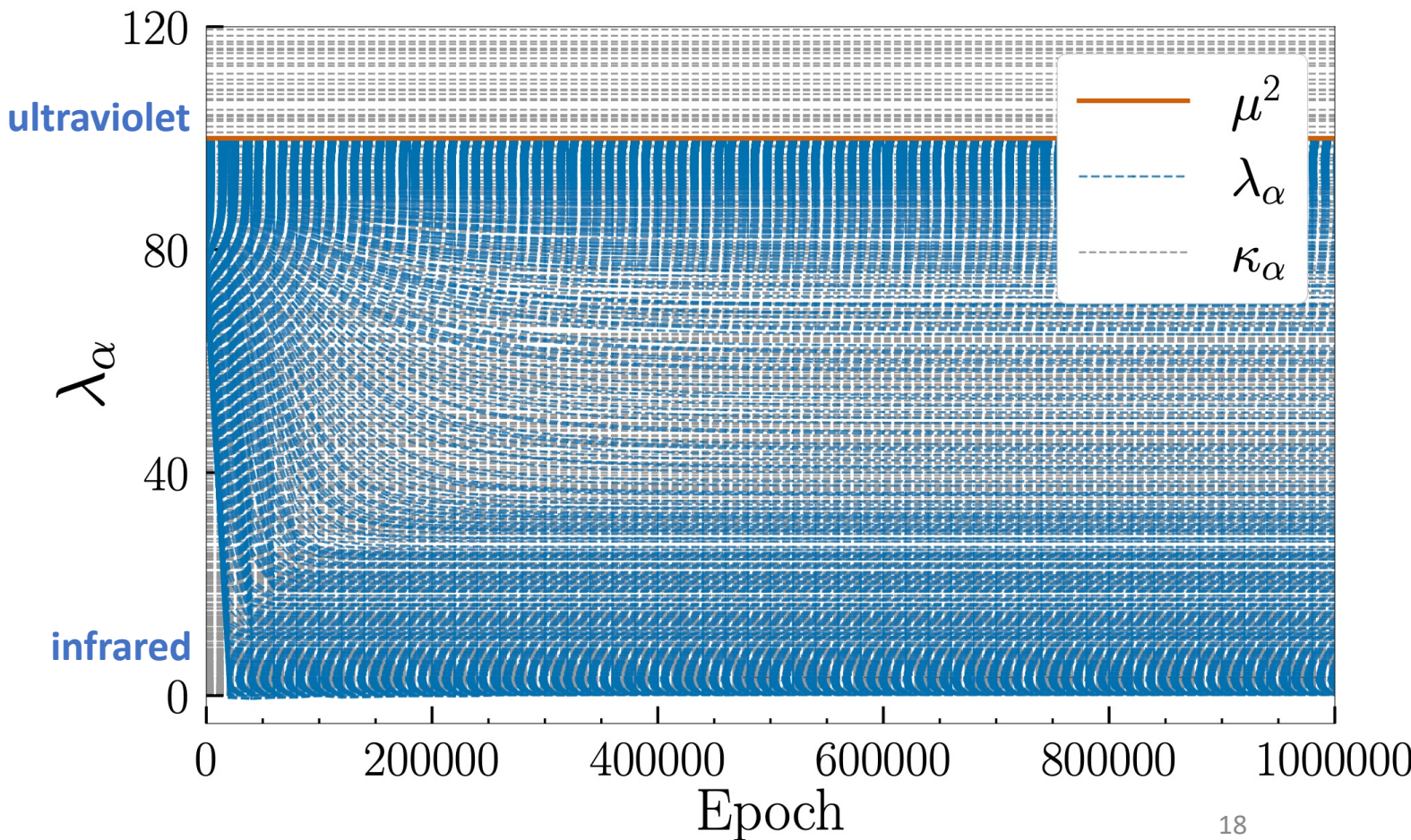


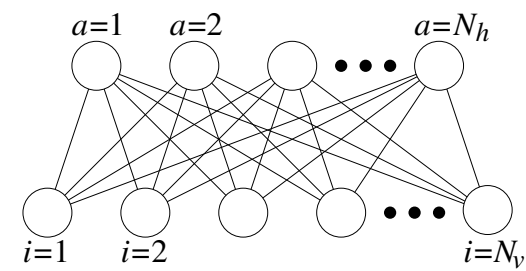
784 eigenvalues



MNIST with fixed RBM mass

- $N_v = N_h = 784$
- fixed RBM parameter $\mu^2 = 100$
- spectrum regulated
- infrared modes learned correctly





MNIST with $N_h \leq N_v$

what is the effect of including incomplete spectrum?



(a) $N_h = 784$



(b) $N_h = 225$



(c) $N_h = 64$

removal of ultraviolet modes affects generative power



(d) $N_h = 36$



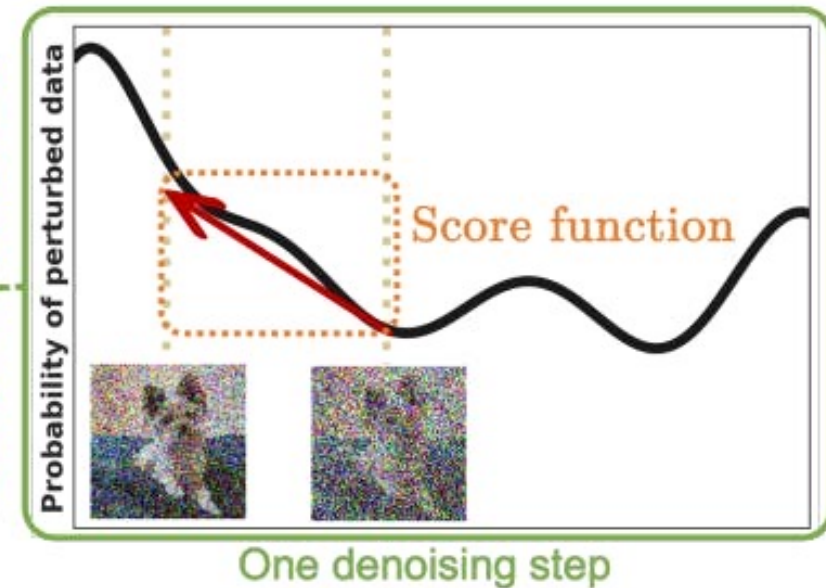
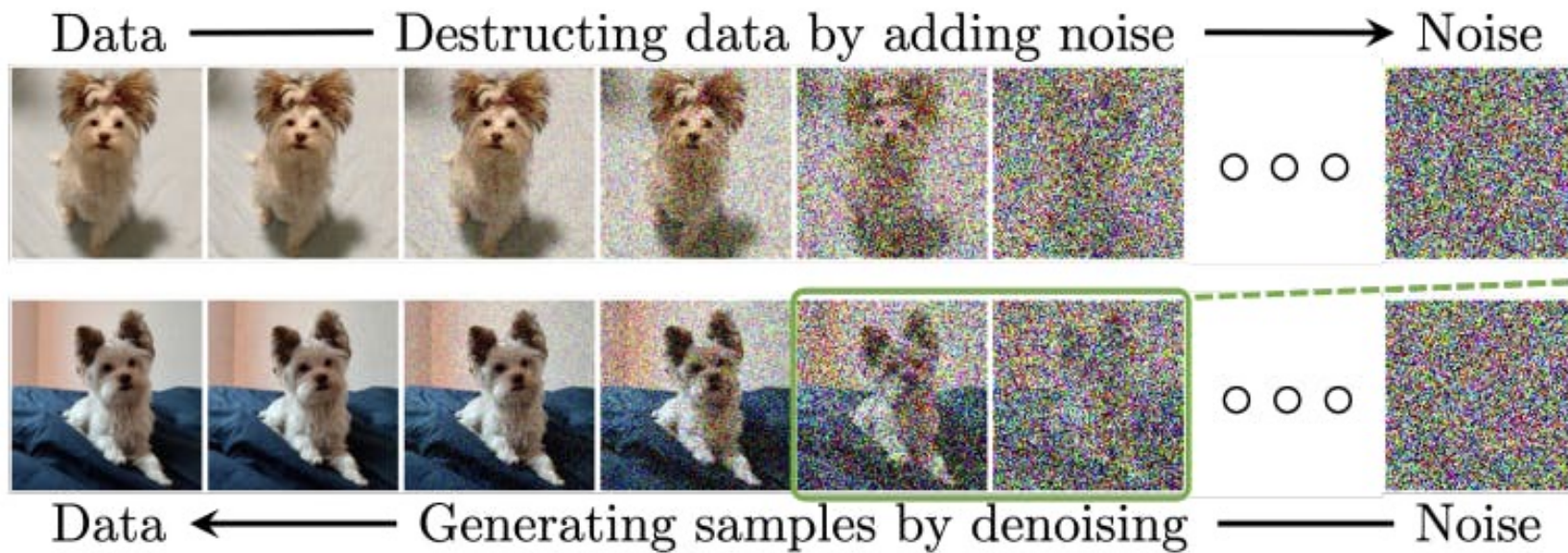
(e) $N_h = 16$



(f) $N_h = 4$

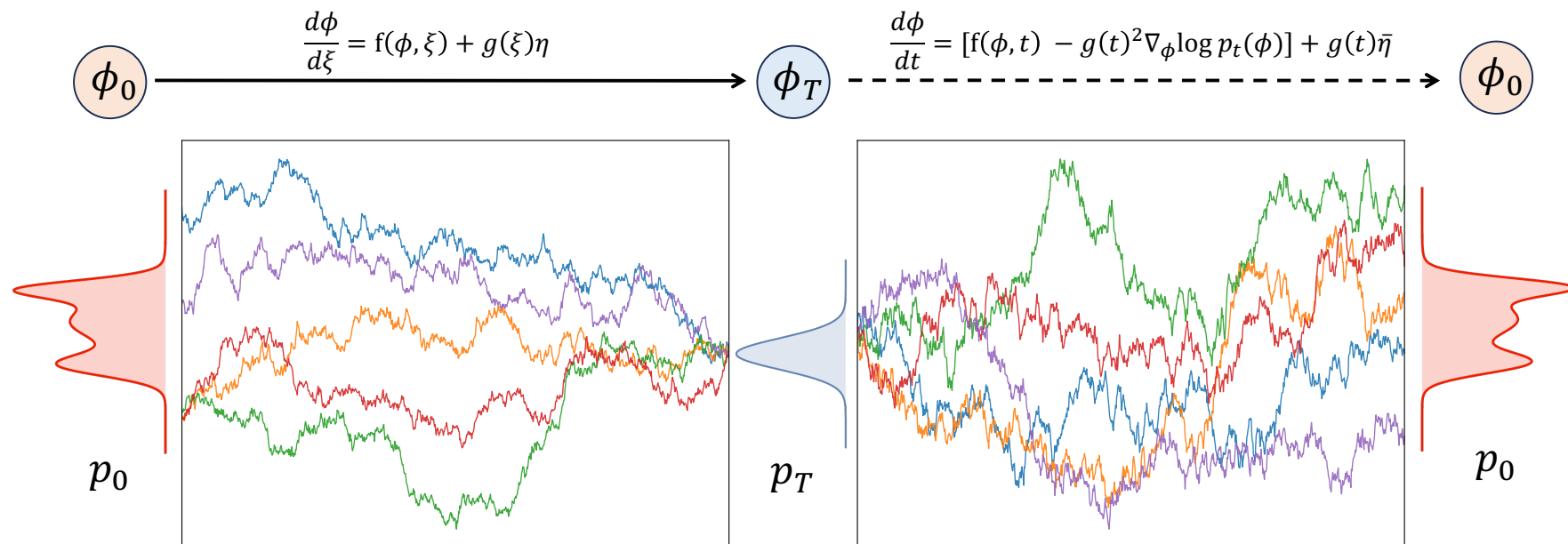
language of quantum fields helps in understanding (at least for me!)

Diffusion models: generative ML



Diffusion models: generative ML

- solve stochastic process with a particular drift/force/score
- drift is learnt during forward diffusion process, starting from data
- new configurations are generated via backward process using learnt drift



Stochastic quantisation

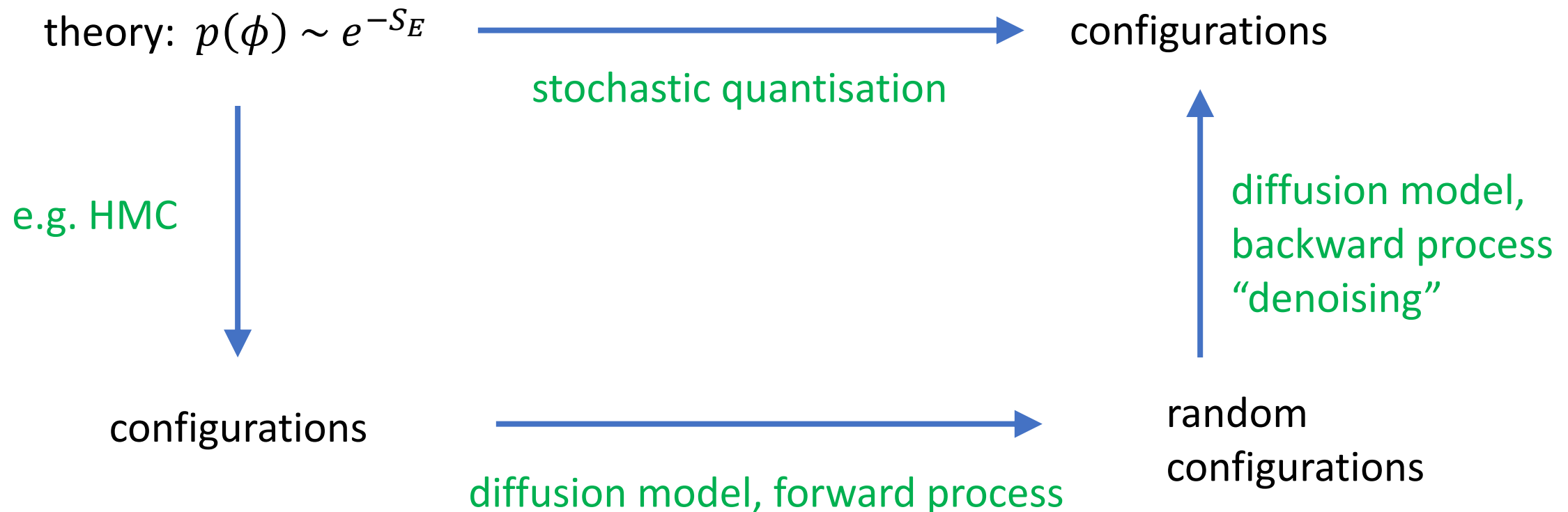
- ideas well-known in quantum field theory: stochastic quantisation (Parisi & Wu 1980)
- path integral quantisation via a stochastic process in fictitious time

$$\frac{\partial \phi(x, \tau)}{\partial \tau} = -\frac{\delta S_E[\phi]}{\delta \phi(x, \tau)} + \eta(x, \tau) \quad \langle \eta(x, \tau) \eta(x', \tau') \rangle = 2\alpha \delta(x - x') \delta(\tau - \tau')$$

- equilibrium solution ($\tau \rightarrow \infty$): distribution $p(\phi) \sim e^{-S_E}$
- convergence guaranteed for real actions due to properties of Fokker-Planck equation
- create samples from Euclidean path integral
- applied to non-abelian gauge theories and QCD in 1980s, but superseded by other methods such as Hybrid Monte Carlo (HMC) [stepsize dependence, efficiency]

Stochastic quantisation and diffusion models

- diffusion models as an alternative approach to stochastic quantisation



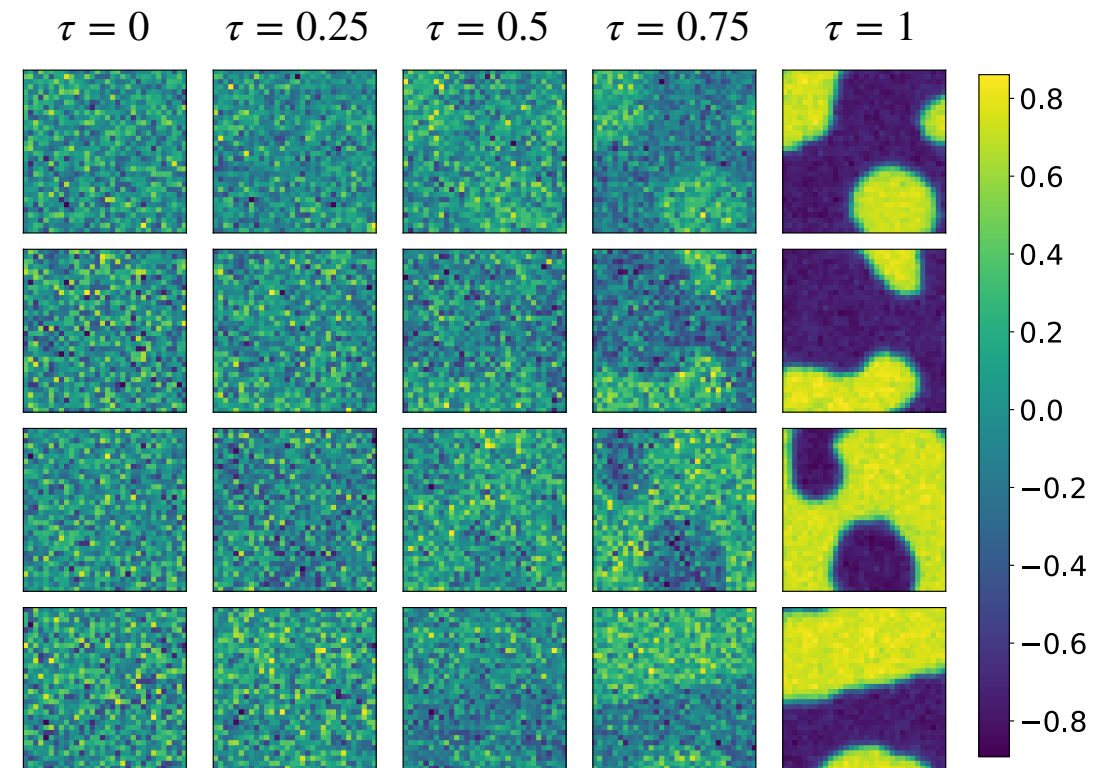
Diffusion model for 2d ϕ^4 scalar theory

- 32^2 lattice, training data set generated using Hybrid Monte Carlo (HMC)
- variance expanding DM trained using U-Net architecture

generating configurations:

- broken phase
- “denoising” (backward process)
- large-scale clusters emerge, as expected

use diffusion models to generate configurations in field theory



Summary: ML in fundamental physics

- lots of applications of ML in particle physics, astronomy, gravitational waves, ...

AI/ML for physics

- considerable overlap between concepts in theoretical physics and in ML
- interesting cross-talk to explore algorithms and improve understanding

physics for AI/ML